

# Analysis of Microarray Data

## Lecture 1: Experimental Design and Data Normalization

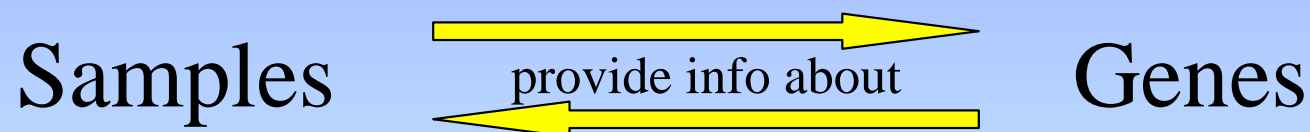
George Bell, Ph.D.  
Senior Bioinformatics Scientist  
Bioinformatics and Research Computing  
Whitehead Institute

# Outline

- Introduction to microarrays
- Experimental design
- Data normalization
- Other data transformation
- Exercises

# Expression microarrays: Underlying assumption and concepts

- Measuring relative changes in levels of specific mRNAs provide information about what's going on in the cells from which the mRNA came.



- A gene expression profile is a molecular phenotype of a cell in a specific state

# Experimental design: Most important question

- Why are you doing this experiment?

(Be as specific as possible.)

“To learn something interesting about my cells” is usually not the best answer.

# Common partial experimental objectives

**Comparison:** identify differentially  
expressed genes

**Discovery:** identify clusters of genes or  
samples

**Prediction:** use a gene expression profile  
to label a cell sample

# General experimental issues

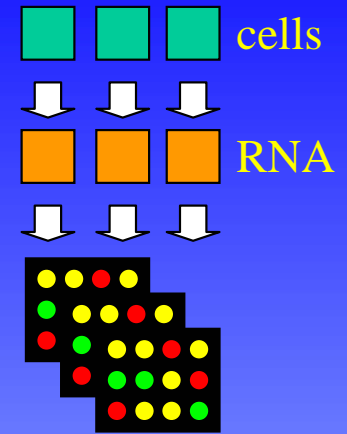
- What is the best source of mRNA?
- Reduce variables as much as possible
- Avoid confounding by randomizing remaining variables
- Collect comprehensive information about all potential variables
- Make no more assumptions than necessary
- Does a factor influence your measurements?  
Collect the data and find out with ANOVA.

# Comparisons

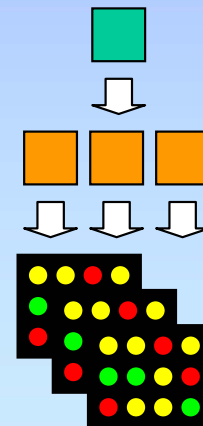
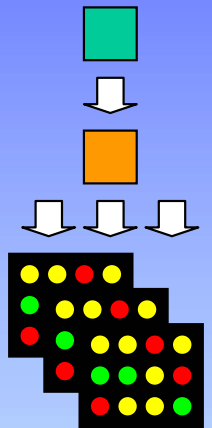
- Virtually all array analysis depends on a comparison between samples (on 3+ chips)
- Expression is usually described in relative terms
- What comparison(s) do you plan to make?
- Research in progress: How can one measure absolute (molar) expression levels?

*Spike-in controls?*

# Replication



- **\*Biological** replicates: use different cell cultures prepared in parallel
- **Technical** replicates: use one cell culture, first processed and then split just before hybridization
- **Sample** replicates: use one cell culture, first split and then processed



\* most informative



# How many replicates?

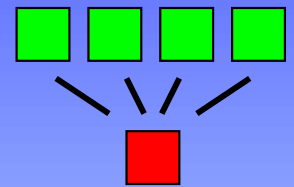
- Replication is needed to have confidence about your results.
- To determine the optimal number using statistics,
  - How large an effect do you want to identify?
  - How confident do you want to be of your conclusions?
  - How variable is gene expression in your system?
  - Perform a test of statistical power (such as ‘power.t.test’ in R)
- Most common practical answer: More than you’ve planned
- If microarray analysis is followed by further confirmation, a high error rate may be tolerated (and may be more efficient)

# Designs for 2-color arrays

Given two replicates of samples A and B,

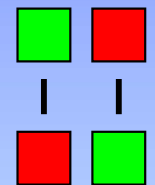
- **Reference design**

A1-R    A2-R            B1-R            B2-R



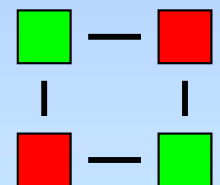
- **Balanced block design**

A1-B1    B2-A2



- **Loop design**

A1-B1    B1-A2            A2-B2            B2-A1



# What design to use?

- Best design depends on objective(s) of experiment
- What comparisons are most important?
- Some guidelines:
  - Balanced block is most efficient for 2-way comparison
  - Reference design is often best when making lots of different comparisons
  - Loop design is not very robust

# Spike-in controls

- How can you confirm that your experiment and analysis was done correctly?
- Control mRNA added before hybridization (or RNA extraction) can help with quality control
- Some chip manufacturers recommend a control mix of exogenous mRNA
- External RNA Control Consortium (ERCC):  
determining optimal control mix to evaluate "reproducibility, sensitivity, and robustness in gene expression analysis"

# Image analysis

- Map region of the chip to a probe and convert its pixels into foreground and background intensities for the spot
- This is a crucial step in the analysis pipeline – but will not be covered in this course
- What instruments and algorithms are recommended by the chip manufacturer?

# Why normalize data?

- The experimental goal is to identify biological variation (expression changes between samples)
- Technical variation can hide the real data
- Unavoidable systematic bias should be recognized and corrected – the process referred to as normalization
- Normalization is necessary to effectively make comparisons between chips – and sometimes within a single chip

# Normalization assumptions and approaches

- Some genes exhibit constant mRNA levels:
  - Housekeeping genes
- The level of some mRNAs are known:
  - Spike-in controls
- The total of all mRNA remains constant:
  - Global median and mean; Lowess
- The distribution of expression levels is constant
  - quantile

# Within-array normalization

- 2-color arrays may need normalization between red and green channels
- These methods are similar to between-array methods
- What should be normalized?
  - Red intensities vs green intensities?
    - Global mean/median
  - Log ratio vs average intensity?
    - Linear regression or loess
- Within-array may be followed by between-array methods



# Normalization by global mean (total intensity)

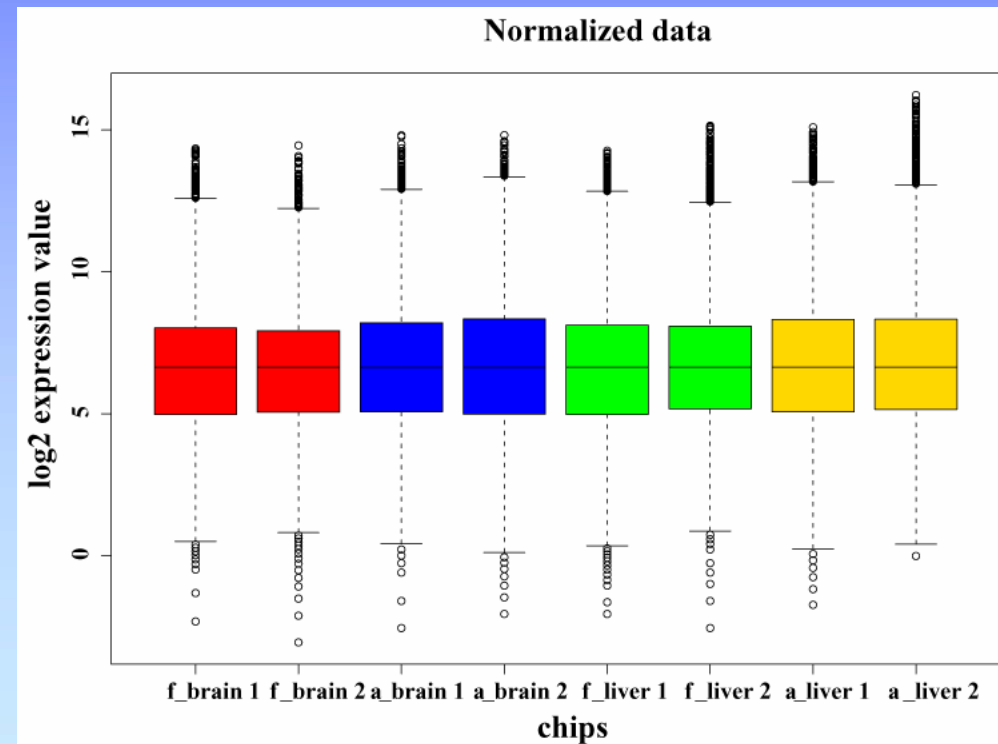
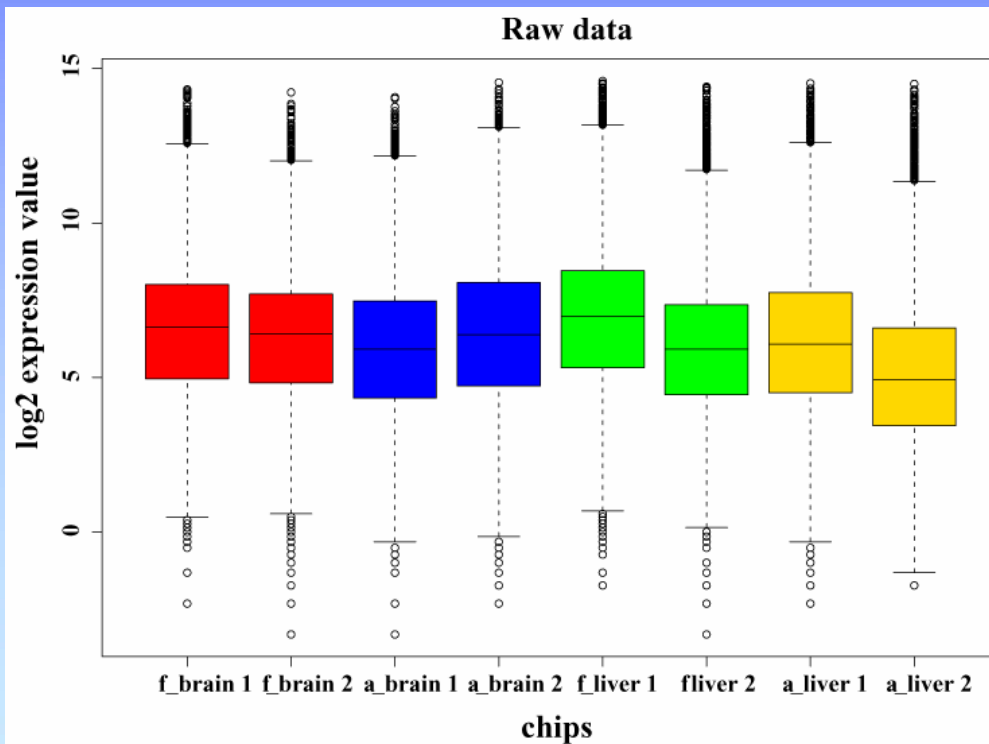
- Procedure: Multiply/divide all expression values for one color (or chip if one-color) by a factor calculated to produce a constant mean (or total intensity) for every color.
- Example with 2 one-color arrays with a total intensity target of 50,000:

Chip	Sample gene expr (raw)	Total expr on chip (raw)	Norm. factor ( $\text{tot}_{\text{des}} / \text{tot}_{\text{obs}}$ )	Sample gene expr (norm)
A	2.0	100,000	$50,000 / 100,000 =$ <b>0.5</b>	$2.0 \times 0.5 =$ 1.000
B	2.2	125,000	$50,000 / 125,000 =$ <b>0.4</b>	$2.2 \times 0.4 =$ 0.88

- Similar scheme can be used with a subset of genes such as with spike-in controls or housekeeping genes

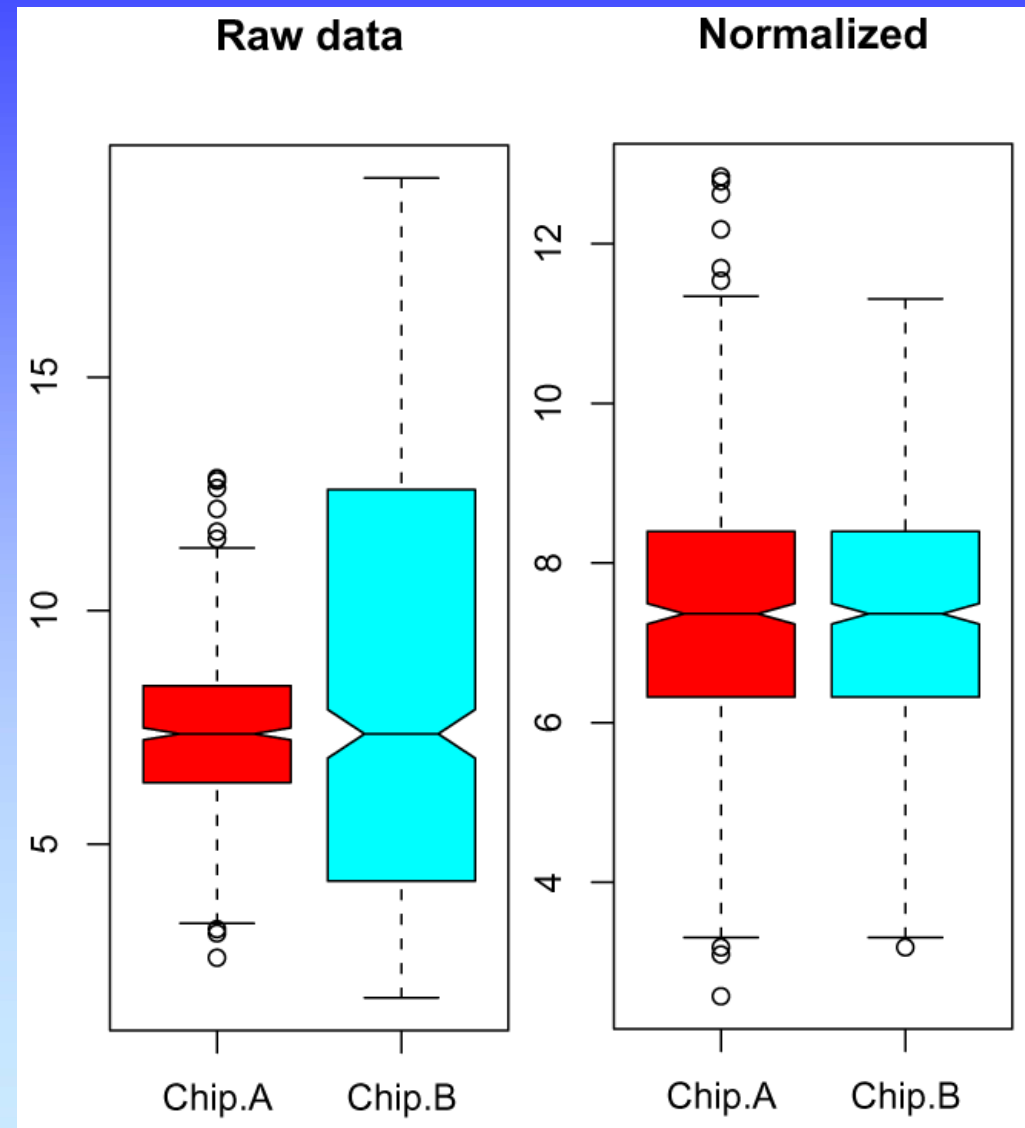
# Global median normalization

- Procedure: Transform all expression values to produce a constant median
- More robust than using the mean



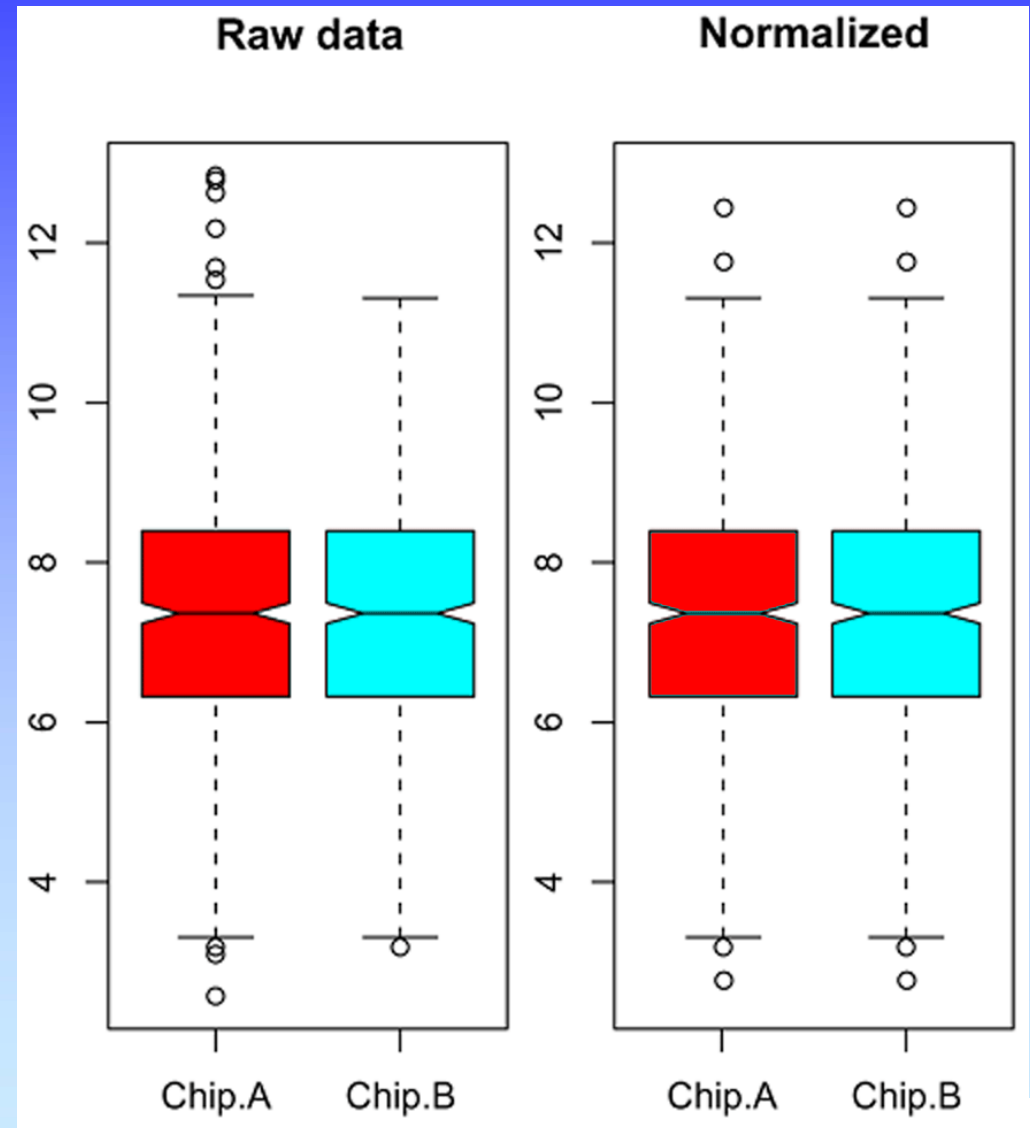
# Variance normalization

- Different chips may have the same median or mean but still very different standard deviations
- If we assume the chips should have common standard deviations, they may be transformed in that manner



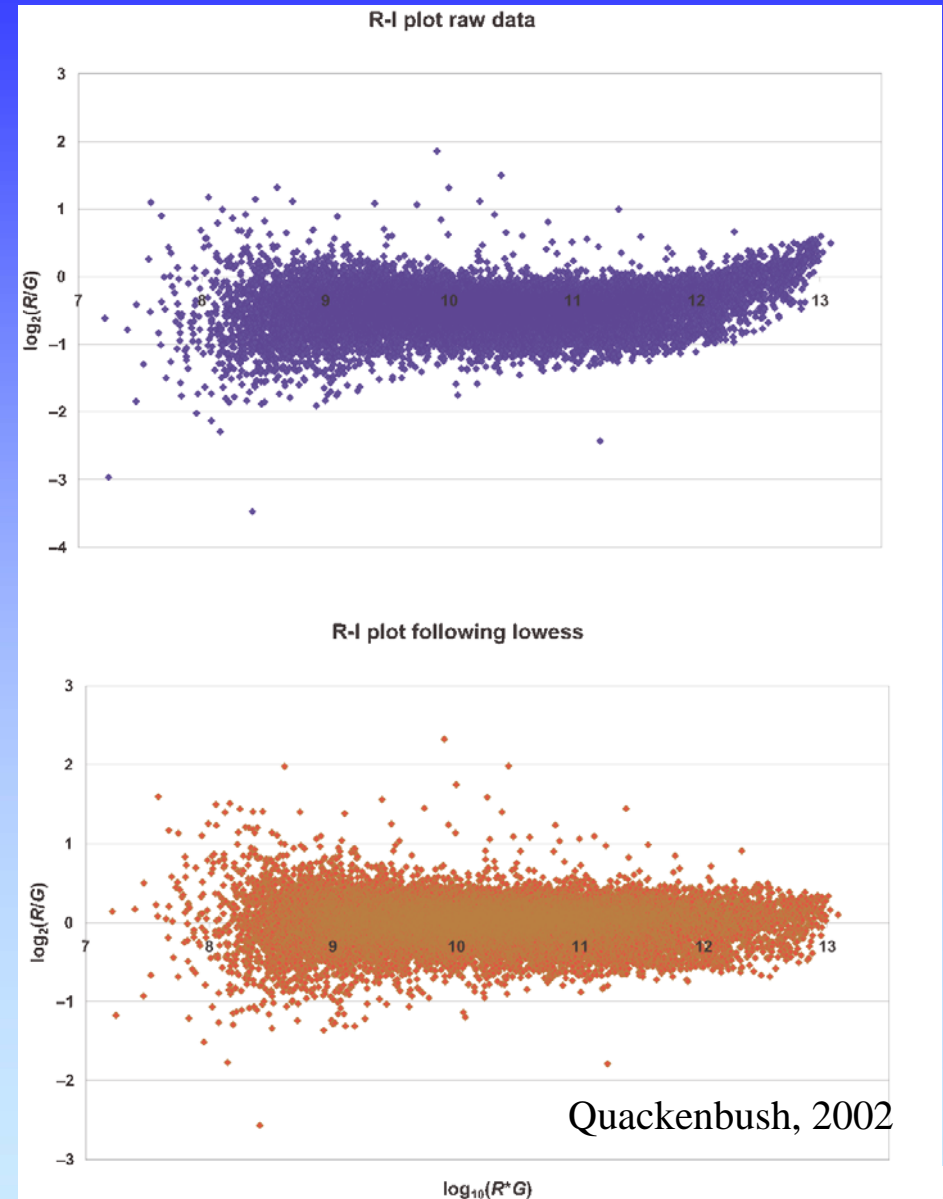
# Quantile normalization

- Different chips may have the same standard deviation but different distributions
- If we assume the chips should have common distributions, they may be transformed in that manner



# Lowess normalization

- Some 2-color arrays exhibit a systematic intensity-dependent bias
- As a result, the normalization factor needs to change with spot intensity
- Lowess (locally weighted scatterplot smoothing) uses local regression to address this



# Local normalization

- Sometimes global within-array normalization may not correct all systematic unwanted variation
- Examples: print tip differences, degradation in chip regions, thumbprints
- Local normalization adjusts intensities according to chip geography
- It's best to avoid technologies that require these “excessive” transformations

# Normalization - summary

- Normalization removes technical variation and improves power of comparisons
- The assumption(s) you make determine the normalization technique to use
- Always look at all the data before and after normalization
- Spike-in controls can help show which method may be best

# Handling low-level values

- What is the background intensity of the chip?
- What expression values are just noise?
- Filtering / flagging low values
- Settings floors and ceilings
- Effects on fold changes and determination of differential expression

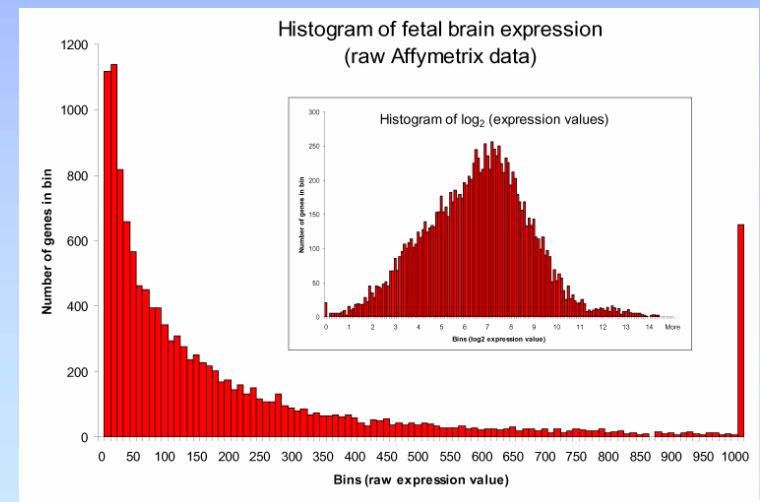


# Affymetrix preprocessing

- Some oligo chip designs (like Affymetrix) represent each gene (“probeset”) with a set of oligos (“probes”).
- Affymetrix software (MAS) uses a special algorithm to convert measurements for a set of probes into one probeset value.
- Other algorithms (RMA, GCRMA, MBEI) have been developed by people who want to improve this calculation.
- These other algorithms appear to increase precision but decrease dynamic range.

# Why use logarithms?

- Produce similar scales for fold changes in both the up and down directions
- Since  $\log(a*b) = \log(a) + \log(b)$ 
  - Multiplicative effects are converted to additive effects, which simplifies statistical analysis
- Produce data with
  - a more normal distribution
  - variability that's not correlated with intensity



# Summary

- Why are you doing a microarray experiment?
- What design will best help address your goal(s)?
- Normalize based on the biology and technology of the experiment
- Other transformations: preprocessing, dealing with low level values; logarithms
- Does your analysis pipeline make sense biologically and statistically?

# References

- Dov Stekel. Microarray Bioinformatics. Cambridge, 2003.
- Churchill, GA. Fundamentals of experimental design for cDNA microarrays. *Nature Genetics Supp.* 32:490-495, 2002.
- Quackenbush J. Microarray data normalization and transformation. *Nature Genetics Supp.* 32:496-501, 2002.
- Smyth GK et al. Statistical issues in cDNA microarray data analysis. *Methods Mol Biol.* 224:111-36, 2003.
- Affymetrix. Statistical Algorithms Description Document. [http://www.affymetrix.com/support/technical/whitepapers/sadd\\_whitepaper.pdf](http://www.affymetrix.com/support/technical/whitepapers/sadd_whitepaper.pdf)
- Irizarry RA et al. Exploration, normalization, and summaries of high density oligonucleotide array probe level data. *Biostatistics* 4(2):249-64, 2003. [RMA]
- Li C and Wong WH. Model-based analysis of oligonucleotide arrays: model validation, design issues and standard error application. *Genome Biol.* 2(8), 2001 [MBEI]
- Wu Z and Irizarry RA. Stochastic models inspired by hybridization theory for short oligonucleotide arrays. *Proceedings of RECOMB '04*. [GCRMA]

# Microarray tools

- Bioconductor (R statistics package)
  - <http://www.bioconductor.org/>
- BaRC analysis tools:
  - [http://iona.wi.mit.edu/bio/tools/bioc\\_tools.html](http://iona.wi.mit.edu/bio/tools/bioc_tools.html)
- Excel
- TIGR MultiExperiment Viewer (MeV)
- Many commercial and open source packages

# Exercise 1 - Excel syntax

A2	Cell reference
A2:A100	Series of cells
=B5	Formula
=\$B\$5	Absolute link ('\$')
=data!B4	Reference other sheet
=[otherFile.xls]data!B4	Reference other file

# Exercise 1: Excel functions

- MEDIAN
- SUM
- AVERAGE
- TRIMMEAN
- LOG
- IF
- TTEST
- VLOOKUP



# The R Project for Statistical Computing

About R  
[What is R?](#)  
[Contributors](#)  
[Screenshots](#)  
[What's new?](#)

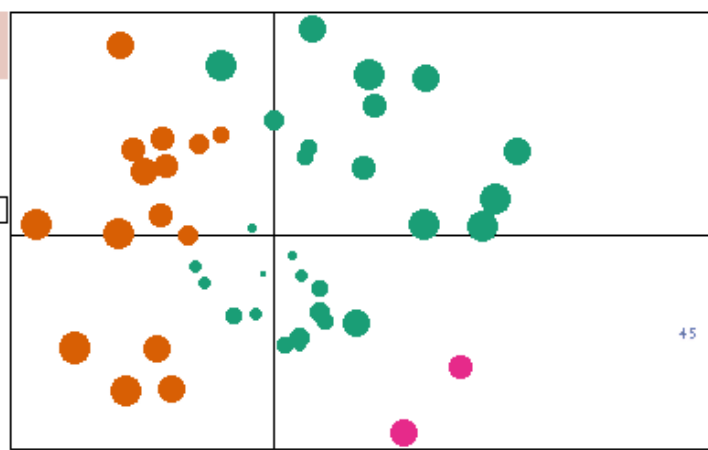
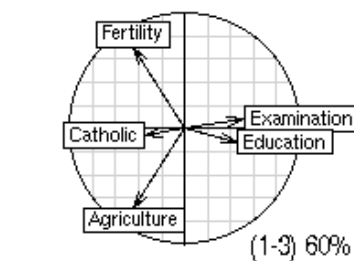
Download  
[CRAN](#)

R Project  
[Foundation](#)  
[Members & Donors](#)  
[Mailing Lists](#)  
[Bug Tracking](#)  
[Developer Page](#)  
[Conferences](#)  
[Search](#)

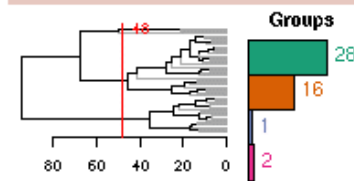
Documentation  
[Manuals](#)  
[FAQs](#)  
[Newsletter](#)  
[Wiki](#)  
[Books](#)  
[Other](#)

Misc  
[Bioconductor](#)  
[Related Projects](#)  
[Links](#)

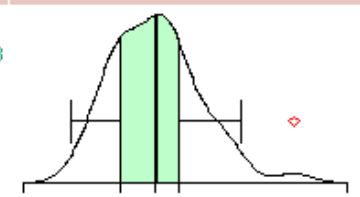
PCA 5 vars  
 princomp(x = data, cor = cor)



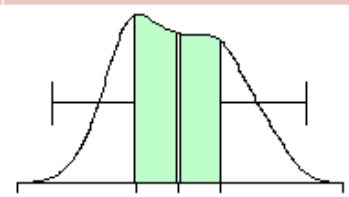
Clustering 4 groups



Factor 1 [41%]



Factor 3 [19%]



**Getting Started:**

- R is a free software environment for statistical computing and graphics. It compiles and runs on a wide variety of UNIX platforms, Windows and MacOS. To download R, please choose your preferred [CRAN mirror](#).
- If you have questions about R like how to download and install the software, or what the license terms are, please read our [answers to frequently asked questions](#) before you send an email.

**News :**

- [R version 2.4.0](#) has been released on 2006-10-03.
- [DSC 2007](#), the 5th workshop on Directions in Statistical Computing, February 15-16, 2007, Auckland, New Zealand.
- [R News 6/4](#) has been published on 2006-10-31.
- The [R Wiki](#) provides an online forum where useRs can help other useRs.



# Introduction to R

# Read a data file

```
dat = read.delim("Data1.txt")
```

```
dim(dat)      # Get dimension of matrix
```

```
colnames(dat) # Get names of columns
```

# Print rows 1-5, columns 2-4

```
dat[1:5, 2:4]      # or use column and row names
```

```
mean(dat[, "my.col.1"]) # get the mean of a column
```

# Combine data by columns

```
all.data = cbind(data1, data2)
```

# Print a tab-delimited text file

```
write.table(all.data, "myFile.txt", sep="\t", quote=F)
```

```
q()      # quit [or use pull-down menu]
```

# Exercise 1 - To do

Goal: Discovery of human developmentally-regulated genes

- Fetal vs adult; liver vs brain; assayed with Affymetrix chips
- Normalize data - 8 chips (replicates)
  - Normalization by trimmed means
  - $k = (\text{expression signal} / \text{chip trimmed mean}) * 100$
- Calculate ratios
  - Reduce data (replicates)
  - Use AVERAGE function
  - Ratio of fetal tissue/adult tissue
- Calculate  $\log_2$  of expression values and ratios